Math 3 Advanced

8.2 Graph Rationals - KEY

Find all the key points of the given rational function.

- 1. $\operatorname{root}(s)$: $x = \frac{3}{2}$ vert. $\operatorname{asymptote}(s)$: x = 2hor. $\operatorname{asymptote}$: y = 2removable discontinuity: $(-4, \frac{11}{6})$
- 3. $\operatorname{root}(s)$: x = 5 $\operatorname{vert. asymptote}(s)$: $x = \frac{1}{2}$ $\operatorname{hor. asymptote}$: $y = \frac{1}{2}$ $\operatorname{removable discontinuity}$: $\left(\frac{2}{3}, -13\right)$
- 5. $\operatorname{root}(\mathbf{s})$: $x = \frac{1}{2}, 3$ vert. $\operatorname{asymptote}(\mathbf{s})$: $x = \frac{2}{3}, 1$ hor. $\operatorname{asymptote}$: $y = \frac{2}{3}$ removable discontinuity: none
- 7. $\operatorname{root}(s)$: x = -3, 2vert. $\operatorname{asymptote}(s)$: x = -2, 1, 4hor. $\operatorname{asymptote}$: y = 0removable discontinuity: none
- 9. root(s): x = -2, 4vert. asymptote(s): x = -5, -3, 3hor. asymptote: y = 0removable discontinuity: none
- 11. $\operatorname{root}(s)$: x = -1, 0, 1vert. $\operatorname{asymptote}(s)$: x = 2, 3hor. $\operatorname{asymptote}$: none removable discontinuity: none

- 2. $\operatorname{root}(s)$: $x = \frac{1}{5}$ vert. $\operatorname{asymptote}(s)$: x = 1hor. $\operatorname{asymptote}$: y = 5removable discontinuity: $\left(-6, \frac{31}{7}\right)$
- 4. root(s): $x = \frac{1}{2}$ vert. asymptote(s): $x = -\frac{1}{3}$ hor. asymptote: $y = \frac{2}{3}$ removable discontinuity: $(1, \frac{1}{4})$
- 6. root(s): $x = -1, \frac{4}{3}$ vert. asymptote(s): $x = -4, -\frac{1}{5}$ hor. asymptote: $y = \frac{3}{5}$ removable discontinuity: none
- 8. $\operatorname{root}(s)$: $x = -1, \frac{1}{2}$ vert. $\operatorname{asymptote}(s)$: x = -5, -3, 2hor. $\operatorname{asymptote}$: y = 0removable discontinuity: none
- 10. $\operatorname{root}(s)$: $x = -\frac{3}{2}, 4$ vert. $\operatorname{asymptote}(s)$: x = -4, 0, 3hor. $\operatorname{asymptote}$: y = 0removable discontinuity: none
- 12. root(s): x = 0, 1vert. asymptote(s): x = -5, 6hor. asymptote: none removable discontinuity: none